

# Core Mathematics C3 Advanced Level

# For Edexcel

## Paper L

**Time: 1 hour 30 minutes**

### *Instructions and Information*

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Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration.

Full marks may be obtained for answers to ALL questions.

The booklet 'Mathematical Formulae and Statistical Tables', available from Edexcel, may be used.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

### *Advice to Candidates*

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You must show sufficient working to make your methods clear to an examiner.  
Answers without working may gain no credit.

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1. Express

$$\frac{x}{x^2 - 9} - \frac{1}{x^2 - 4x + 3}$$

as a single fraction in its simplest form.

(6)

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2. The function  $f$  is given by

$$f: x \mapsto e^{2x+3}, \quad x \in \mathbb{R}.$$

(a) Find the exact value of  $ff(0)$ .

(2)

(b) Find an expression for  $f^{-1}(x)$ .

(3)

(c) Write down the domain of  $f^{-1}$ .

(1)

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3. Given that

$$x = \ln(y^2 + 4),$$

show that  $\frac{dy}{dx} = \frac{y}{2} + \frac{2}{y}$ .

(6)

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4.  $f(x) = \ln x - 3x + 5, \quad x > 0$

(a) Show that there is a root  $\alpha$  of  $f(x) = 0$  in the interval  $[1, 2]$ .

(2)

The root  $\alpha$  is to be estimated using the iterative formula

$$x_{n+1} = \frac{1}{3}(\ln x_n + 5), \quad x_0 = 2.$$

(b) Calculate the values of  $x_1, x_2, x_3$  and  $x_4$  giving your answers to 4 significant figures.

(3)

(c) Prove that  $\alpha$  is 1.876, to 4 significant figures.

(2)

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5. (a) Given that  $y = \tan x + \sin 2x$ , find the value of  $\frac{dy}{dx}$  at  $x = \frac{\pi}{4}$ .

(4)

(b) Find the equation of the tangent to the curve at the point where  $x = \frac{\pi}{4}$ .

(3)

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6. (a) Prove that

$$\sin 2\theta \equiv \frac{2 \tan \theta}{1 + \tan^2 \theta}. \quad (4)$$

(b) Hence solve the equation

$$\tan \theta(4 - \tan \theta) = 1, \quad 0 < \theta < \frac{\pi}{2}. \quad (5)$$

7.

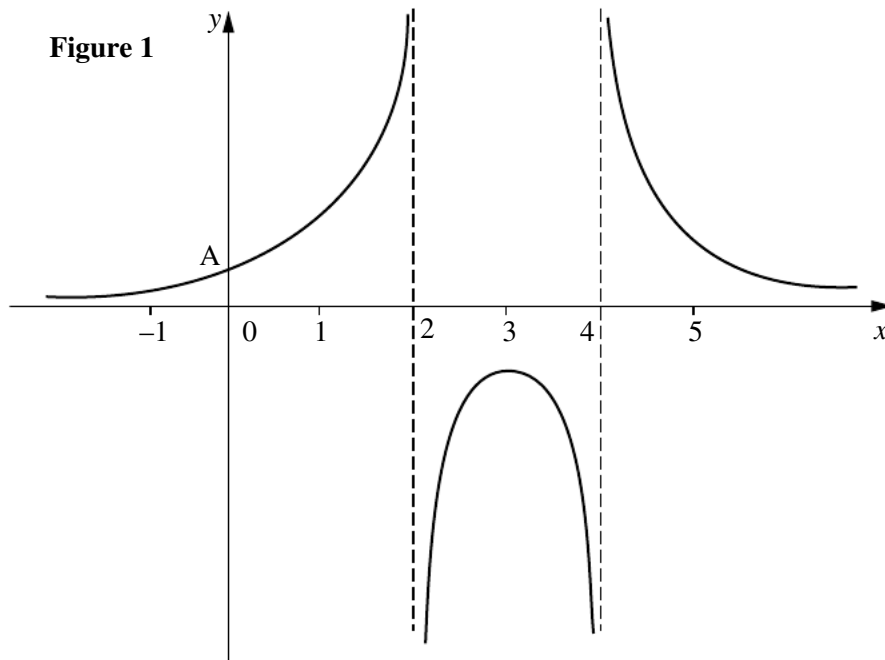


Figure 1 shows a sketch of the curve with the equation  $y = f(x)$ ,  $x \in \mathbb{R}$ .

The curve has a maximum point at  $(3, -1)$  and meets the  $y$ -axis at the point  $A(0, 0.125)$ .

The lines  $x = 2$ ,  $x = 4$  and the  $x$  axis are asymptotes to the curve as shown in Fig. 1.

On a separate diagram sketch the graphs of

(a)  $y = |4f(x)|$  (5)

(b)  $y = f(x + 3)$  (4)

In each case show clearly

- (i) the coordinates of any points at which the curve has a maximum or minimum point,
- (ii) how the curve approaches the asymptotes of the curve,
- (iii) the coordinates of  $A$ .

8. (a) On the same pair of axes sketch the graphs of  
 $y = |x - a|$  and  $y = 2a - |x - a|$  where  $a > 0$ . Label the graphs clearly. (5)
- (b) Write down the coordinates of the points of intersection of the two graphs. (2)
- (c) Find the area of the quadrilateral formed. (3)
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9. (a) Express  $\cos \theta + 2 \sin \theta$  in the form  $R \cos(\theta - \alpha)$ , where  $R > 0$  and  $0 < \alpha < \frac{\pi}{2}$ .  
Give the values of  $R$  and  $\alpha$  to 3 significant figures. (4)
- (b) Find the maximum and minimum values of  $\cos \theta + 2 \sin \theta$  and the smallest possible value for  $\theta$  for which the maximum occurs. (2)

The depth  $d$  metres, of water in a lake is modelled using the equation

$$d = 15 + \cos\left(\frac{\pi t}{12}\right) + 2 \sin\left(\frac{\pi t}{12}\right), \quad 0 \leq t < 24,$$

where  $t$  hours is the number of hours after 1200.

- (c) Calculate the maximum depth of water predicted by this model and the value of  $t$  when this maximum occurs. (4)
- (d) Calculate the depth of the water at 1200. (1)
- (e) Calculate, to the nearest half hour, the time in the evening when the depth of the water is 15 metres. (4)
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**END**

**TOTAL 75 MARKS**